

## ECTS catalog with learning outcomes University of Montenegro

## Faculty of Science and Mathematics / PHYSICS / MATHEMATICS I

| Course:                          | MATHEMATICS I   |          |              |                                       |  |  |  |  |  |
|----------------------------------|---|----------|--------------|---------------------------------------|--|--|--|--|--|
| Course ID                        | Course status   | Semester | ECTS credits | Lessons (Lessons+Execises+Laboratory) |  |  |  |  |  |
| 1310                             | Mandatory   | 1        | 8            | 3+3+0                                 |  |  |  |  |  |
| Programs                         | PHYSICS   |          |              |                                       |  |  |  |  |  |
| Prerequisites                    |   |          |              |                                       |  |  |  |  |  |
| Aims                             | The aim of the course is mastering the basics of mathematical analysis: the notion of convergence, practical methods for calculation of limit values, elements of differential calculus and its applications in the graphics drawing functions.   |          |              |                                       |  |  |  |  |  |
| Learning outcomes                | After passing this exam, the student should be able to 1. Defines the notion of convergent sequence and successfully use various techniques for finding the limit values and prove the convergence of a sequence. 2. Find limit values of functions and determines intervals of their continuity. 3. Make a graph of basic and complex functions. 4. Determines derivatives of basic and complex functions. 5. Use derivatives and The Mean Value Theorem to solve some practical problems in physics, as well as the maximum and minimum problems. |          |              |                                       |  |  |  |  |  |
| Lecturer / Teaching<br>assistant | Vladimir Božović and Dušica Slović  |          |              |                                       |  |  |  |  |  |
| Methodology                      | Lectures, exercises, independent work, and consultations.   |          |              |                                       |  |  |  |  |  |
| Plan and program of<br>work      |   |          |              |                                       |  |  |  |  |  |
| Preparing week                   | Preparation and registration of the semester  |          |              |                                       |  |  |  |  |  |
| I week lectures                  | Review - notion of a sequence, Arithmetic and Geometric sequence.   |          |              |                                       |  |  |  |  |  |
| I week exercises                 | Review - notion of a sequence, Arithmetic and Geometric sequence.   |          |              |                                       |  |  |  |  |  |
| II week lectures                 | The notion of convergence, Convergent sequences - definition and examples   |          |              |                                       |  |  |  |  |  |
| II week exercises                | The notion of convergence, Convergent sequences - definition and examples   |          |              |                                       |  |  |  |  |  |
| III week lectures                | Properties of convergent sequences, Monotone sequences, Number e as a limit of the sequence   |          |              |                                       |  |  |  |  |  |
| III week exercises               | Properties of convergent sequences, Monotone sequences, Number e as a limit of the sequence   |          |              |                                       |  |  |  |  |  |
| IV week lectures                 | Some interesting application of sequences - Examples in Physics   |          |              |                                       |  |  |  |  |  |
| IV week exercises                | Some interesting application of sequences - Examples in Physics   |          |              |                                       |  |  |  |  |  |
| V week lectures                  | The nootion of series - series as a sequence, Properties of series  |          |              |                                       |  |  |  |  |  |
| V week exercises                 | The nootion of series - series as a sequence, Properties of series  |          |              |                                       |  |  |  |  |  |
| VI week lectures                 | The limit of a function, Calculating limits using the limit laws  |          |              |                                       |  |  |  |  |  |
| VI week exercises                | The limit of a function, Calculating limits using the limit laws  |          |              |                                       |  |  |  |  |  |
| VII week lectures                | The precise definition of a limit, Continuity   |          |              |                                       |  |  |  |  |  |
| VII week exercises               | The precise definition of a limit, Continuity   |          |              |                                       |  |  |  |  |  |
| VIII week lectures               | Midterm exam  |          |              |                                       |  |  |  |  |  |
| VIII week exercises              | Midterm exam  |          |              |                                       |  |  |  |  |  |
| IX week lectures                 | Derivatives, The derivative as a function, Derivatives of elementary functions  |          |              |                                       |  |  |  |  |  |
| IX week exercises                | Derivatives, The derivative as a function, Derivatives of elementary functions  |          |              |                                       |  |  |  |  |  |
| X week lectures                  | The Chain Rule, Derivatives of functions in implicit and parametric form  |          |              |                                       |  |  |  |  |  |
| X week exercises                 | The Chain Rule, Derivatives of functions in implicit and parametric form  |          |              |                                       |  |  |  |  |  |
| XI week lectures                 | Applications of differentiation, Maximum and minimum values, The Mean Value Theorem   |          |              |                                       |  |  |  |  |  |
| XI week exercises                | Applications of differentiation, Maximum and minimum values, The Mean Value Theorem   |          |              |                                       |  |  |  |  |  |
| XII week lectures                | How derivatives affect the shape of a graph, Indeterminate forms and L'Hospital's rule, Review  |          |              |                                       |  |  |  |  |  |
| XII week exercises               | How derivatives affect the shape of a graph, Indeterminate forms and L'Hospital's rule, Review  |          |              |                                       |  |  |  |  |  |
| XIII week lectures               | Taylor and Maclaurin Series   |          |              |                                       |  |  |  |  |  |
| XIII week exercises              | Taylor and Maclaurin  | Series   |              |                                       |  |  |  |  |  |



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|--|---------------------|---|---|---|---|---|---------------------------------------|--|--|
| XIV week le  | ctures              | Monotonicity, convexity and inflection points of differentiable functions, Graphing functions |   |   |   |   |                                       |  |  |
| XIV week ex  | xercises            | Monotonicity, convexity and inflection points of differentiable functions, Graphing functions |   |   |   |   |                                       |  |  |
| XV week led  | ctures              | Makeup exam   |   |   |   |   |                                       |  |  |
| XV week ex   | ercises             | Makeup exam   |   |   |   |   |                                       |  |  |
| Student w  | orkload             |   |   |   |   |   |                                       |  |  |
| Per week   |                     |   | Per semester  |   |   |   |                                       |  |  |
| 8 credits x 40/30=10 hours and 40 minuts 3 sat(a) theoretical classes 0 sat(a) practical classes 3 excercises 4 hour(s) i 40 minuts of independent work, including consultations |                     |   | Classes and final exam:  10 hour(s) i 40 minuts x 16 =170 hour(s) i 40 minuts  Necessary preparation before the beginning of the semester (administration, registration, certification):  10 hour(s) i 40 minuts x 2 =21 hour(s) i 20 minuts  Total workload for the subject:  8 x 30=240 hour(s)  Additional work for exam preparation in the preparing exam period, including taking the remedial exam from 0 to 30 hours (remaining time from the first two items to the total load for the item)  48 hour(s) i 0 minuts  Workload structure: 170 hour(s) i 40 minuts (cources), 21 hour(s) i 20 minuts (preparation), 48 hour(s) i 0 minuts (additional work) |   |   |   |                                       |  |  |
| Student obligations  |                     |   | Students are encouraged to attend classes regularly, although this is not mandatory. However, it is doubtful that one will do well in the course if you miss too many lectures.   |   |   |   |                                       |  |  |
| Consultations  |                     |   | As agreed with the professor or teaching assistant.   |   |   |   |                                       |  |  |
| Literature   |                     |   | 1. Z. Kaldeburg, V. Mićić, S. Ognjanović, Analiza sa algebrom III, "Krug"<br>Beograd, 2000. 2. James Stewart, Early Transcendentals 6, ISBN-13:<br>978-0-495-01166-8, 2008.   |   |   |   |                                       |  |  |
| Examination methods  |                     |   | The forms of testing and grading 1. Midterm exam (up to 45 points) and Final exam (up to 45 points). 2. The points awarded for special commitment (up to 10 points). Grading scale: F (below 50 points), E (50-59 points), D (60-69), C (70-79), B (80-8  |   |   |   |                                       |  |  |
| Special remarks  |                     |   |   |   |   |   |                                       |  |  |
| Comment  |                     |   | If opportunity to take a makeup test, or correctional final exam is used, then the results achieved on them will be treated as definitive.  |   |   |   |                                       |  |  |
| Grade:   | F                   | Е   |   | D   | С   | В   | А                                     |  |  |
| Number<br>of points  | less than 50 points | greater th<br>equal to 5<br>and less t<br>points  | 0 points  | greater than or<br>equal to 60 points<br>and less than 70<br>points | greater than or<br>equal to 70 points<br>and less than 80<br>points | greater than or<br>equal to 80 points<br>and less than 90<br>points | greater than or<br>equal to 90 points |  |  |
|  | ·                   |   |   |   |   |   |                                       |  |  |