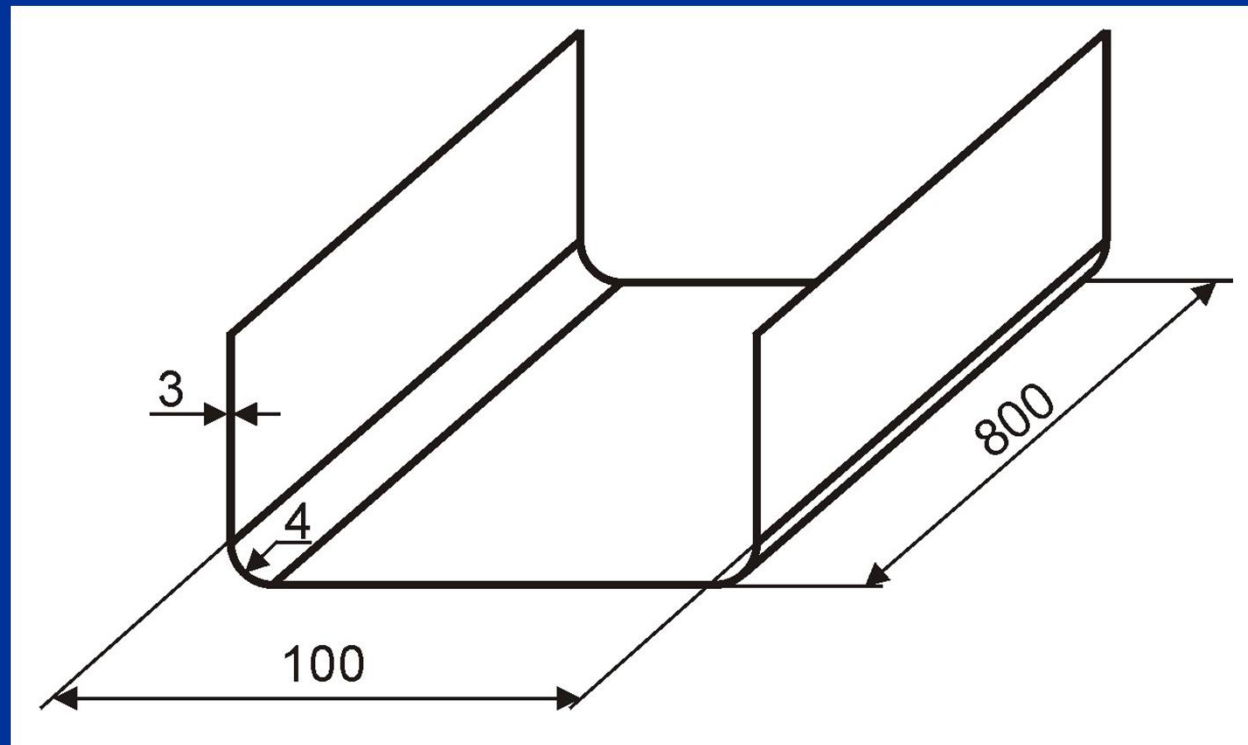


5. Domaći zadatak - Savijanje

Za slučaj savijanja dijela na slici:

- dati raspored radijalnih i tangecionalnih napona,
- izračunati potrebnu silu za savijanje komada.

Uslovi: $\sigma_T = 600 [N / mm^2]$



Slika 5.1.

PRORAČUN:

1. Raspored radijalnih i tangencionalnih napona

$$s = 3[mm]$$

$$r = 4[mm]$$

$$a = 100[mm]$$

$$b = 800[mm]$$

$$\sigma_T = 600[N/mm^2]$$

$$\rho_n = \sqrt{R \cdot r} = \sqrt{7 \cdot 4} = 5.29[mm]$$

ρ_n - poluprečnik krivine neutralne naponske linije,

$$R = r + s = 4 + 3 = 7[mm]$$

R - spoljni radijus,

$$k = \sigma_T = 600[N/mm^2]$$

Radijalni naponi u zoni sabijanja (pritiska)

$$\sigma_{\rho_s} = -k \ln \frac{\rho}{r}$$

$$\begin{aligned}\rho_1 = r = 4[mm] & \quad \sigma_{\rho_{s1}} = -600 \ln \frac{4}{4} = 0 \\ \rho_2 = 4.5[mm] & \quad \sigma_{\rho_{s2}} = -600 \ln \frac{4.5}{4} = -70.66[N/mm^2] \\ \rho_3 = 5[mm] & \quad \sigma_{\rho_{s3}} = -600 \ln \frac{5}{4} = -133.88[N/mm^2] \\ \rho_4 = 5.29[mm] & \quad \sigma_{\rho_{s4}} = -600 \ln \frac{5.29}{4} = -167.71[N/mm^2]\end{aligned}$$

Radijalni naponi u zoni istezanja

$$\sigma_{\rho_i} = -k \ln \frac{R}{\rho}$$

$$\begin{aligned}\rho_5 = 5.29[mm] & \quad \sigma_{\rho_{i5}} = -600 \ln \frac{7}{5.29} = -168.05[N/mm^2] \\ \rho_6 = 6[mm] & \quad \sigma_{\rho_{i6}} = -600 \ln \frac{7}{6} = -92.49[N/mm^2] \\ \rho_7 = 6.5[mm] & \quad \sigma_{\rho_{i7}} = -600 \ln \frac{7}{6.5} = -44.46[N/mm^2] \\ \rho_8 = 7[mm] & \quad \sigma_{\rho_{i8}} = -600 \ln \frac{7}{7} = 0\end{aligned}$$

Tangencijalni naponi u zoni sabijanja (pritiska)

$$\sigma_{\varphi} = -k(1 + \ln \frac{\rho}{r})$$

$$\rho_1 = r = 4[mm] \quad \sigma_{\varphi_{s1}} = -600(1 + \ln \frac{4}{4}) = -600[N/mm^2]$$

$$\rho_2 = 4.5[mm] \quad \sigma_{\varphi_{s2}} = -600(1 + \ln \frac{4.5}{4}) = -670.67[N/mm^2]$$

$$\rho_3 = 5[mm] \quad \sigma_{\varphi_{s3}} = -600(1 + \ln \frac{5}{4}) = -733.89[N/mm^2]$$

$$\rho_4 = 5.29[mm] \quad \sigma_{\varphi_{s4}} = -600(1 + \ln \frac{5.29}{4}) = -767.71[N/mm^2]$$

Tangencijalni naponi u zoni istezanja

$$\sigma_{\varphi} = k(1 - \ln \frac{R}{\rho})$$

$$\rho_5 = 5.29[mm] \quad \sigma_{\varphi_{i5}} = 600(1 - \ln \frac{7}{5.29}) = 431.94[N/mm^2]$$

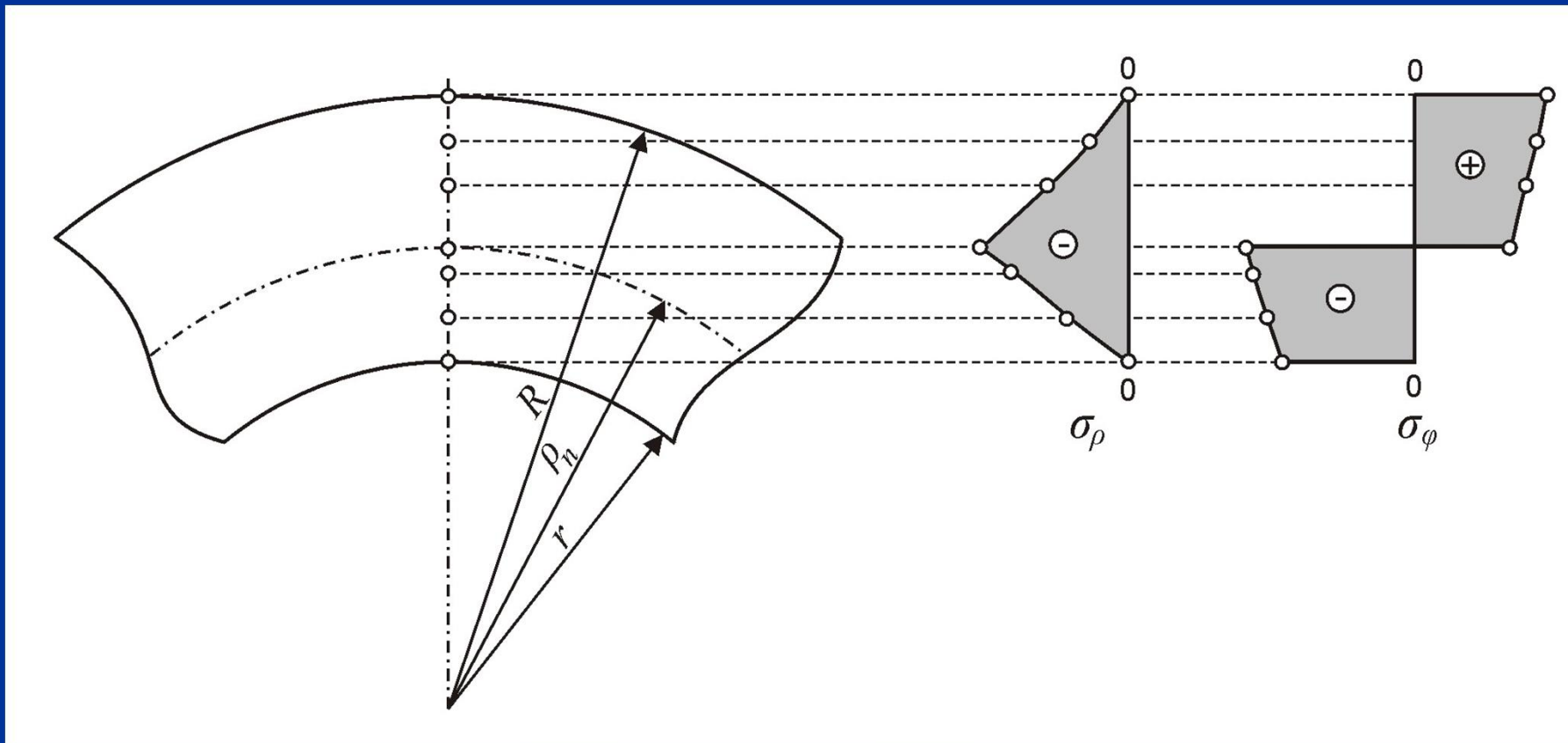
$$\rho_6 = 6[mm] \quad \sigma_{\varphi_{i6}} = 600(1 - \ln \frac{7}{6}) = 507.50[N/mm^2]$$

$$\rho_7 = 6.5[mm] \quad \sigma_{\varphi_{i7}} = 600(1 - \ln \frac{7}{6.5}) = 555.53[N/mm^2]$$

$$\rho_8 = 7[mm] \quad \sigma_{\varphi_{i8}} = 600(1 - \ln \frac{7}{7}) = 600[N/mm^2]$$

ρ [mm]	4	4.5	5	5.29	6	6.5	7
σ_ρ [N/mm ²]	0	-70.66	-133.88	-167.71 -168.50	-92.49	-44.46	0
σ_φ [N/mm ²]	-600	-670.67	-733.89	-767.71 431.9	507.50	555.53	600

Dijagram rasporeda radijalnih i tangencionalnih napona



2. Proračun sile

$$F = \frac{(1 + \sin \alpha) b \cdot s^2}{2l} \sigma_T$$

$$l = r_1 + r_2 + s = 2r + s = 2 \cdot 4 + 3 = 11 [\text{mm}]$$

$$r_1 = r_2 = r$$

r_1 - radijus pritiskivača,

r_2 - radijus matrice,

$$\text{Za } \alpha = 0^\circ \Rightarrow \sin \alpha = 0, \quad F_{\min} = \frac{b \cdot s^2}{2l} \sigma_T = \frac{800 \cdot 3^2}{2 \cdot 11} 600 = 196363.36 [\text{N}] = 196.4 [\text{kN}]$$

$$\text{Za } \alpha = 90^\circ \Rightarrow \sin \alpha = 1, \quad F_{\max} = \frac{2 \cdot b \cdot s^2}{2l} \sigma_T = \frac{800 \cdot 3^2}{11} 600 = 392727.27 [\text{N}] = 392.8 [\text{kN}]$$

Ukupna deformaciona sila

$$F_s = F + F_i + F_r$$

F_i - sila izbacivača, $F_i = 0.3 \cdot F$

F_r - sila ravnjanja, $F_r = p \cdot A$

$A = (a - 2 \cdot r)b = (100 - 2 \cdot 4)800 = 73600 [\text{mm}^2]$ - površina ravnjanja,

$$F_s = 1.3 \frac{b \cdot s^2}{l} \sigma_T + p \cdot A = 1.3 \frac{800 \cdot 3^2}{11} 600 + 100 \cdot 73600 = 7870548.45 [\text{N}] = 7870.5 [\text{kN}]$$