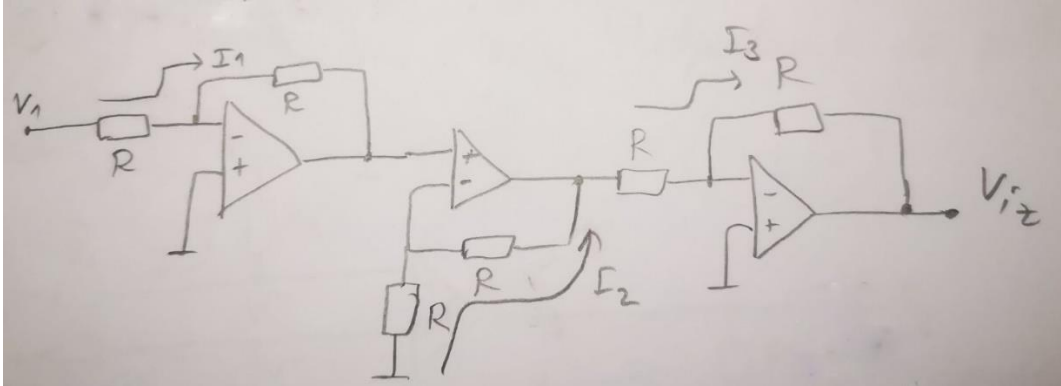


OPERACIONI POJAČAVAČI

1. Za kolo na slici izračunati izlazni napon. Poznato je $V_1 = 8V$, $R = 4k\Omega$, $V_{CC} = \pm 12V$.



Rješenje:

$$V_1^+ = V_1^- = 0V$$

$$V_2^+ = V_2^-$$

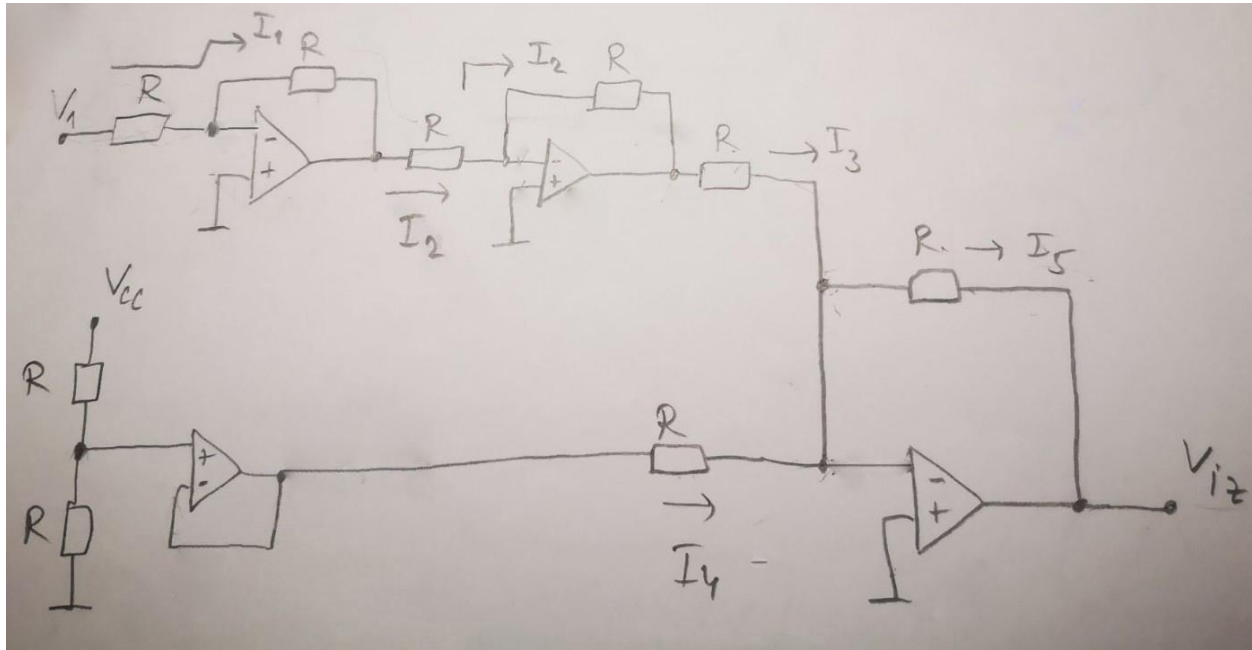
$$V_3^+ = V_3^- = 0V$$

$$I_1 = \frac{V_1 - V_1^-}{R} = \frac{V_1^- - V_{1z}}{R} \quad \text{tj.} \quad \frac{V_1}{R} = \frac{-V_{1z}}{R} \rightarrow V_{1z} = -V_1 = -8V \rightarrow V_{1z} = V_2^+ = V_2^- = -8V$$

$$I_2 = \frac{-V_2^-}{R} = \frac{V_2^- - V_{2z}}{R} \rightarrow V_{2z} = 2V_2^- = -16V \text{ (zasićenje)} \rightarrow V_{2z} = -12V$$

$$I_3 = \frac{V_{2z} - V_3^-}{R} = \frac{V_3^- - V_{iz}}{R} \quad \text{tj.} \quad \frac{V_{2z}}{R} = \frac{-V_{iz}}{R} \rightarrow V_{iz} = -V_{2z} = 12V$$

2. Za kolo na slici operacioni pojačavači se napajaju sa $V_{CC} = \pm 6V$. Poznato je $V_1 = -4V$ i $R = 1k\Omega$. Odrediti izlazni napon.



Rješenje:

$$I_1 = \frac{V_1}{R} = \frac{-V_{1z}}{R} \rightarrow V_{1z} = -V_1 = 4V$$

$$I_2 = \frac{V_{1z}}{R} = \frac{-V_{2z}}{R} \rightarrow V_{2z} = -4V$$

$$I_3 = \frac{V_{2z}}{R} = \frac{-4V}{R}$$

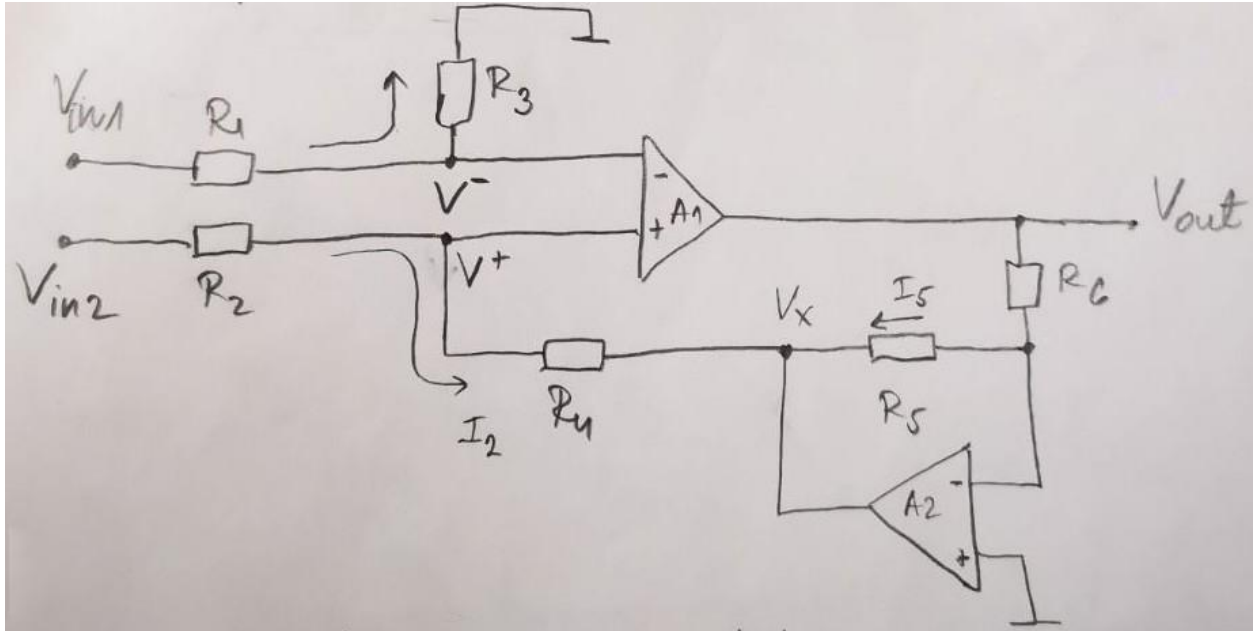
$$V_4^+ = \frac{R}{R+R} V_{CC} = \frac{V_{CC}}{2} = 3V \rightarrow V_4^+ = V_{4z} = 3V$$

$$I_4 = \frac{V_{4z}}{R} = \frac{3V}{R}$$

$$\text{Za čvor važi } I_3 + I_4 = I_5 \rightarrow I_5 = \frac{-4V}{R} + \frac{3V}{R} = \frac{-1V}{R}$$

$$\text{S druge strane } I_5 = \frac{-V_{iz}}{R} \text{ pa slijedi da je } V_{iz} = 1V.$$

3. Za kolo na slici izračunati izlazni napon. Poznato je $\frac{R_1}{R_3} = \frac{R_2}{R_4}$, $R_5, R_6, V_{in1}, V_{in2}$. Pretpostaviti da su operacioni pojačavači idealni.



Rješenje:

$$V^+ = V^-$$

$$\frac{V_{in1} - V^-}{R_1} = \frac{V^-}{R_3} \quad (1) \rightarrow V^- = \frac{R_3}{R_1 + R_3} V_{in1} \quad (2) \rightarrow V^+ = \frac{R_3}{R_1 + R_3} V_{in1} \quad (3)$$

Dalje imamo da je $\frac{V_{in2} - V^+}{R_2} = \frac{V^+ - V_x}{R_4}$ (4) pri čemu ako u izraz (4) uvrstimo (3) dobijamo:

$$\frac{V_{in2} - \frac{R_3}{R_1 + R_3} V_{in1}}{R_2} = \frac{\frac{R_3}{R_1 + R_3} V_{in1} - V_x}{R_4} \quad (5) \text{ . Sređivanjem dobijamo:}$$

$$V_x = \frac{R_3}{R_1 + R_3} V_{in1} - R_4 \left(\frac{V_{in2} - \frac{R_3}{R_1 + R_3} V_{in1}}{R_2} \right) = \frac{R_3}{R_1 + R_3} V_{in1} - \frac{R_4}{R_2} V_{in2} + \frac{R_4}{R_2} \frac{R_3}{R_1 + R_3} V_{in1} \rightarrow$$

$$V_x = \frac{R_3}{R_1 + R_3} V_{in1} \left(1 + \frac{R_4}{R_2} \right) - \frac{R_4}{R_2} V_{in2} \quad (6)$$

Dalje sa slike vidimo da je $\frac{V_{out}}{R_6} = \frac{-V_x}{R_5} \rightarrow V_{out} = \frac{-R_6 V_x}{R_5}$ (7) pa uvrštavanjem (6) u (7)

dobijamo: $V_{out} = \frac{-R_6}{R_5} \left(\frac{R_3}{R_1 + R_3} V_{in1} \left(1 + \frac{R_4}{R_2} \right) - \frac{R_4}{R_2} V_{in2} \right) =$

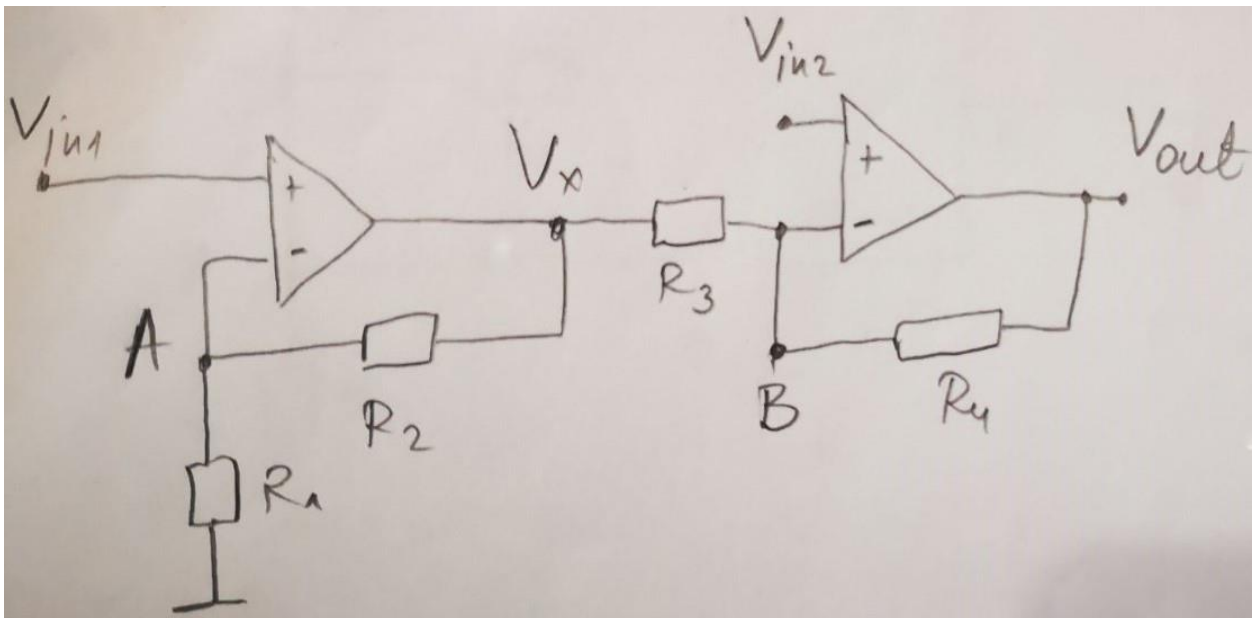
$$V_{out} = \frac{R_6}{R_5} \left(\frac{1}{\frac{R_2}{R_4}} V_{in2} - \frac{1}{\frac{R_1}{R_3} + 1} V_{in1} \left(1 + \frac{1}{\frac{R_2}{R_4}} \right) \right) \quad (8)$$

Uvrštavanjem $\frac{R_1}{R_3} = \frac{R_2}{R_4}$ u (8) dobijamo:

$$V_{out} = \frac{R_6}{R_5} \left(\frac{1}{\frac{R_2}{R_4}} V_{in2} - \frac{1}{\frac{R_2}{R_4} + 1} V_{in1} \left(1 + \frac{1}{\frac{R_2}{R_4}} \right) \right) = \frac{R_6}{R_5} \left(\frac{1}{\frac{R_2}{R_4}} V_{in2} - V_{in1} \frac{1}{\frac{R_2}{R_4} + 1} \left(\frac{\frac{R_2}{R_4} + 1}{\frac{R_4}{R_2}} \right) \right)$$

$$V_{out} = \frac{R_6}{R_5} \left(\frac{1}{\frac{R_2}{R_4}} V_{in2} - V_{in1} \frac{1}{\frac{R_2}{R_4}} \right) = \frac{R_6}{R_5} \frac{R_4}{R_2} (V_{in2} - V_{in1})$$

4. a) Odrediti kakav odnos treba da bude između otpornosti R_1 , R_2 , R_3 i R_4 da bi kolo radilo kao instrumentacioni pojačavač.
- b) Ako se između tačaka A i B priključi otpornik R_5 odrediti V_{out} pri $R_1=R_2=R_3=R_4$.



Rješenje:

a) Za prvi operacioni pojačavač važi $V_1^+ = V_1^- = V_{in1}$ (1)

$$\frac{-V_1^-}{R_1} = \frac{V_1^- - V_X}{R_2} \quad (2) \rightarrow V_X = (1 + \frac{R_2}{R_1})V_1^- \rightarrow V_X = (1 + \frac{R_2}{R_1})V_{in1} \quad (3)$$

Za drugi operacioni pojačavač važi $V_2^+ = V_2^- = V_{in2}$ (4)

$$\frac{V_X - V_2^-}{R_3} = \frac{V_2^- - V_{out}}{R_4} \quad (5)$$

$$\text{Uvrštanjem (4) i (3) u (5) dobijamo: } \rightarrow \frac{(1 + \frac{R_2}{R_1})V_{in1} - V_{in2}}{R_3} = \frac{V_{in2} - V_{out}}{R_4} \quad (6) \rightarrow$$

$$V_{out} = V_{in2} - R_4 \frac{(1 + \frac{R_2}{R_1})V_{in1} - V_{in2}}{R_3} = V_{in2} (1 + \frac{R_4}{R_3}) - \frac{R_4}{R_3} (1 + \frac{R_2}{R_1})V_{in1} \quad (7)$$

Da bi kolo radilo kao instrumentacioni pojačavač izlazni napon mora biti jednak:

$$V_{out} = k(V_{in2} - V_{in1}) \quad (8)$$

Primjenjujući uslov (8) u jednačini (7) dobijamo da je:

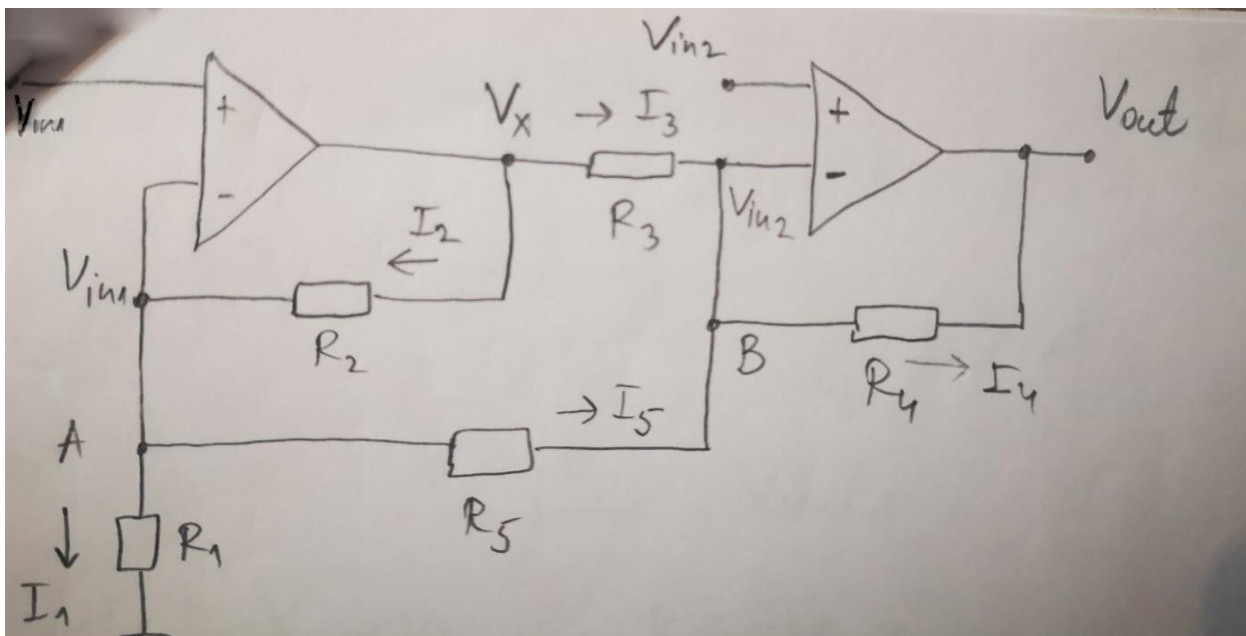
$$(1 + \frac{R_4}{R_3}) = k \quad (9)$$

$$\frac{R_4}{R_3} (1 + \frac{R_2}{R_1}) = k \quad (10)$$

Izjednačavajući izraze (9) i (10) dobijamo:

$$(1 + \frac{R_4}{R_3}) = \frac{R_4}{R_3} (1 + \frac{R_2}{R_1}) \rightarrow \frac{R_4}{R_3} \frac{R_2}{R_1} = 1 \rightarrow \frac{R_4}{R_3} = \frac{R_1}{R_2}$$

b) Ako se doda otpornik između tačaka A i B kolo postaje:



Za čvor A važi da je $I_2 = I_1 + I_5$ (1)

$$\frac{V_x - V_{in1}}{R_2} = \frac{V_{in1}}{R_1} + \frac{V_{in1} - V_{in2}}{R_5} \quad (2) \rightarrow$$

$$V_x = V_{in1} + \frac{R_2 V_{in1}}{R_1} + \frac{R_2 (V_{in1} - V_{in2})}{R_5} = V_{in1} \frac{R_1 R_5 + R_2 R_5 + R_1 R_2}{R_1 R_5} - \frac{R_2}{R_5} V_{in2} \quad (3)$$

Za čvor B važi da je $I_3 + I_5 = I_4$ (4)

$$\frac{V_x - V_{in2}}{R_3} + \frac{V_{in1} - V_{in2}}{R_5} = \frac{V_{in2} - V_{out}}{R_4} \quad (5) \rightarrow V_{out} = V_{in2} - R_4 \left(\frac{V_x - V_{in2}}{R_3} + \frac{V_{in1} - V_{in2}}{R_5} \right) \rightarrow$$

$$V_{out} = -\frac{R_4}{R_3} V_x + V_{in2} \left(1 + \frac{R_4}{R_3} + \frac{R_4}{R_5} \right) - \frac{R_4}{R_5} V_{in1} \quad (6)$$

Uvrštavanjem (3) u (6) dobijamo:

$$V_{out} = -\frac{R_4}{R_3} \left(V_{in1} \frac{R_1 R_5 + R_2 R_5 + R_1 R_2}{R_1 R_5} - \frac{R_2}{R_5} V_{in2} \right) + V_{in2} \left(1 + \frac{R_4}{R_3} + \frac{R_4}{R_5} \right) - \frac{R_4}{R_5} V_{in1}$$

$$V_{out} = \frac{R_4}{R_3} \left(\frac{R_2}{R_5} V_{in2} - V_{in1} \frac{R_1 R_5 + R_2 R_5 + R_1 R_2}{R_1 R_5} \right) + V_{in2} \left(1 + \frac{R_4}{R_3} + \frac{R_4}{R_5} \right) - \frac{R_4}{R_5} V_{in1}$$

$$V_{out} = V_{in2} \left(\frac{R_4}{R_3} \frac{R_2}{R_5} + 1 + \frac{R_4}{R_3} + \frac{R_4}{R_5} \right) - V_{in1} \left(\frac{R_4}{R_3} \frac{R_1 R_5 + R_2 R_5 + R_1 R_2}{R_1 R_5} + \frac{R_4}{R_5} \right) \quad (7)$$

Primjermom uslova zadatka da je $R_1 = R_2 = R_3 = R_4$, u izraz (7) dobijamo:

$$V_{out} = 2V_{in2} \left(\frac{R_1}{R_5} + 1 \right) - 2V_{in1} \left(1 + \frac{R_1}{R_5} \right) = 2 \left(1 + \frac{R_1}{R_5} \right) (V_{in2} - V_{in1})$$